

**Katwa College**  
**Department of Physics**  
**Internal Examination – 2024**  
**B.Sc (Hons) Semester – V CBCS**  
**Paper – DSE – 1 (Advanced Mathematical Physics)**

**Time: 1hr.**

**F.M.- 10**

**Answer any five**

- 1. Prove that the eigen-values of any Hermitian matrix are real.**
- 2. Prove that orthogonal matrices must be non-singular.**
- 3. Prove that sum of the eigen-values of any matrix is equal to the trace of that matrix.**
- 4. Prove that the product of the eigen-values of any matrix is equal to the determinant of the matrix.**
- 5. Find the eigen-values of  $\sigma_x$  and  $\sigma_y$ ;  $\sigma_x$  and  $\sigma_y$  are pauli spin matrices.**
- 6. If  $\lambda$  be the eigen-value of a non-singular matrix A, belonging to the eigen-vector  $x$ , what will be the eigen-value of  $A^{-1}$ ?**
- 7. Prove trace of a matrix remains invariant under similarity transformation.**